# Consistency in Non-Transactional Distributed Storage Systems

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Over the years, different meanings have been associated to the word *consistency* in the distributed systems community. While in the '80s "consistency" typically meant *strong consistency*, later defined also as *linearizability*, in recent years, with the advent of highly available and scalable systems, the notion of "consistency" has been at the same time both weakened and blurred.

In this paper we aim to fill the void in literature, by providing a structured and comprehensive overview of different consistency notions that appeared in distributed systems, and in particular *storage* systems research, in the last four decades. We overview more than 50 different consistency notions, ranging from linearizability to eventual and weak consistency, defining precisely many of these, in particular where the previous definitions were ambiguous. We further provide a partial order among different consistency predicates, ordering them by their semantic "strength", which we believe will reveal useful in future research. Finally, we map the consistency semantics to different practical systems and research prototypes.

The scope of this paper is restricted to non-transactional semantics, i.e., those that apply to single storage object operations. As such, our paper complements the existing surveys done in the context of transactional, database consistency semantics.

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## 1. INTRODUCTION

Faced with the inherent challenges of failures, communication/computation asynchrony and concurrent access to shared resources, distributed system designers have continuously sought to hide these fundamental concerns from users by offering abstractions and semantic models of various strength. At first glance, the ultimate goal of a distributed system is seemingly simple, as it should ideally be just a fault-tolerant and more scalable version of a centralized system. Namely, an ideal distributed system should leverage distribution and replication to boost availability by masking failures, provide scalability and/or reduce latency, but maintain the simplicity of use of a centralized system – and, notably, its *consistency* – providing the illusion of sequential access. Such *strong* consistency criteria can be found in early seminal works that paved the way of modern storage systems, e.g., [Lamport 1978; Lamport 1986a], as well as in the subsequent advances in defining general, practical correctness conditions, such as *linearizability* [Herlihy and Wing 1990].

Unfortunately, the goals of high availability and strong consistency, in particular linearizability, have been identified as mutually conflicting in many practical circum-

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stances. Negative theoretical results and lower bounds, such as the FLP impossibility result [Fischer et al. 1985] and the CAP theorem [Gilbert and Lynch 2002], shaped the design space of distributed systems. As a result, distributed system designers have either to give up the idealized goals of scalability and availability, or relax consistency.

In recent years, the rise of commercial Internet-scale wide area computing caused system designers to prefer availability over consistency, leading to the advent of weak and eventual consistency [Terry et al. 1994; Saito and Shapiro 2005; Vogels 2008]. Consequently, much research has been focusing on attaining a better understanding of those weaker semantics [Bailis and Ghodsi 2013], but also on adapting [Bailis et al. 2014] or dismissing and replacing stronger ones [Helland 2007]. Along this line of research, tools have been conceived in order to deal with consistency at the level of programming languages [Alvaro et al. 2011], data objects [Shapiro et al. 2011a; Burckhardt et al. 2012] or data flows [Alvaro et al. 2014].

Today, however, after roughly four decades of intensive and exciting research on various flavors of consistency, we lack a structured and comprehensive overview of different consistency notions that appeared in distributed systems research, and *storage* systems research, in particular.

This paper aims to help fill this void, by giving an overview of over 50 different consistency notions, ranging from linearizability to eventual and weak consistency, defining precisely many of these, in particular where the previous definitions were ambiguous. We further provide a partial order among different consistency notions, ordering them by their semantic "strength", which we believe will reveal useful in further research. Finally, we map the consistency semantics to different practical systems and research prototypes. The scope of this paper is restricted to non-transactional semantics that apply to single storage object operations. We focus on non-transactional storage systems as they have become increasingly popular in recent years due to their simple implementations and good scalability. As such, our paper complements the existing surveys done in the context of transactional, database consistency semantics (see, e.g., [Adya 1999]), which we omit for space limitations.

This survey is organized as follows. In Section 2 we define our model of a distributed system and set up the framework for reasoning about different consistency semantics. In order to ensure the broadest coverage of our work, we model the distributed system as asynchronous, i.e., without predefined constraints on timing of computation and communication. Our framework, which we derive from the work of Burckhardt [2014], captures the dynamic aspects of a distributed system, through *histories* and *abstract executions* of such systems. We define an execution as a set of actions (i.e., *operations*) invoked by some processes on the storage objects through their interface. To analyze executions we adopt the notion of history, i.e., the set of operations of a given execution. Leveraging the information attached to the history, we are able to properly capture the intrinsic complexity of executions. Namely, we can group and relate operations according to their features (e.g., by the processes and objects they refer to, and by their timings), or by the dynamic relationships established during executions (e.g., causality). Additionally, abstract executions augment histories with orderings of operations that account for the resolution of write conflicts and their propagation within the storage system.

Section 3 brings the main contribution of our paper: a survey of more than 50 different consistency semantics proposed in the context of non-transactional distributed

storage systems. We define many of these models employing the framework specified in Section 2, i.e., using declarative compositions of logic predicates over graph entities. In turn, these definitions enable us to establish the hierarchical partial order of consistency semantics according to their semantic strengths (given in Figure 1 of Section 3). For better readability, we also loosely classify consistency semantics into ten *families*, which group them by their common traits.

We discuss our work in the context of related consistency surveys in Section 4 and conclude in Section 5. We further complement our survey with a summary of all consistency predicates defined in this work (Appendix A). In addition, for all consistency models mentioned in this work, we provide references to their original, primary definitions, as well as pointers to research papers that propose related implementations (Appendix B). Specifically, we reference implementations that appeared in recent proceedings of the most relevant venues. We believe that this is a useful contribution on its own, as it will allow distributed systems researchers and, in particular, students, to navigate more easily through the very large number of research papers that deal with different subtleties of consistency.

#### 2. SYSTEM MODEL

In this section, we specify the main notions behind the reasoning about consistency semantics carried out in the rest of this paper. We rely on the concurrent objects abstraction, as presented by Lynch and Tuttle [1989] and by Herlihy and Wing [1990], for the definitions of fundamental "static" elements of the system, such as objects and processes. Moreover, to reason about dynamic behaviors of the system (i.e., executions), we build upon the mathematical framework laid out in [Burckhardt 2014].

#### 2.1. Preliminaries

Objects and Processes. We consider a distributed system consisting of a finite set of processes, modeled as I/O automata [Lynch and Tuttle 1989], interacting with shared (or concurrent) objects through a fully connected asynchronous communication network. Unless stated otherwise, processes and shared objects (or, simply, objects) are correct, i.e., they do not fail. Each process and object is identified by a unique identifier. We define ProcessIds as the set of all process identifiers and ObjectIds as the set of all object identifiers.

Additionally, each object has a unique object type. Depending on the type, the object can assume values belonging to a defined domain denoted by Values, and it supports a set of primitive operation types (i.e.,  $OpTypes = \{rd, wr, inc, \ldots\}$ ) that provide the only means to manipulate that object. For simplicity and without loss of generality, unless specified otherwise, in this work we further classify operations as either reads (rd) or writes (wr). Namely, we model as a write (or update) any operation that modifies the value of the object, while, conversely, reads return to the caller the current value held by the object's replica without causing any change to it. We adopt the term object replicas, or simply replicas, to refer to the different copies of a same named shared object maintained in the storage system for fault tolerance or performance enhancement. Ideally, replicas of the same shared object should hold the same data at any time. The coordination protocols among replicas are however determined by the implementation of the shared object.

<sup>&</sup>lt;sup>1</sup>Note that, while this paper focuses on survey of consistency semantics proposed in the context of distributed storage, our approach maintains generality as our consistency definitions are applicable to other replicated data structures beyond distributed storage.

<sup>&</sup>lt;sup>2</sup>For readability, we adopt a notation in which a set *Values* is implicitly parametrized by object type.

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*Time*. Unless specified otherwise, we assume an asynchronous computation and communication model, with no bounds on computation and communication latencies. However, when describing certain consistency semantics, we will be using terms such as *recency* or *staleness*. Such terms relate to the concept of *real time*, i.e., an ideal and global notion of time that we use to reason about histories a posteriori, although it is not accessible by processes during executions. We refer to the real time domain as Time, which we model as the set of positive real numbers, i.e.,  $\mathcal{R}^+$ .

## 2.2. Operations, Histories and Abstract Executions

*Operations*. We describe an operation issued by a process on a shared object as the tuple (*proc*, *type*, *obj*, *ival*, *oval*, *stime*, *rtime*), where:

- $proc \in ProcessIds$  is the id of the process invoking the operation.
- $-type \in OpTypes$  is the operation type.
- $-obj \in ObjectIds$  is the id of the object on which the operation is invoked.
- $-ival \in Values$  is the operation input value.
- $oval \in Values \cup \{\nabla\}$  is the operation output value, or  $\nabla$  if the operation does not return.
- $-stime \in Time$  is the operation invocation time.
- $-rtime \in Time \cup \{\Omega\}$  is the operation return time, or  $\Omega$  if the operation does not return.

By convention, we use the special value  $\sqcup \in Values$  to represent the input value (i.e., ival) of reads and, possibly, the return value (i.e., oval) of writes. For simplicity, given operation op, we will use the notation op.par to access its parameter named par as expressed in the tuple (e.g., op.type represents its type, and op.ival its input value).

*Histories.* A history H is a set of operations. Intuitively, a history contains all operations invoked in a given execution. We further denote by  $H|_{wr}$  (resp.,  $H|_{rd}$ ) the set of write (resp., read) operations of a given history H (e.g.,  $H|_{wr} = \{op \in H : op.type = wr\}$ ). We further define the following relations on elements of a history:

- rb (returns-before) is a natural partial order on H based on real-time precedency. Formally:  $rb \triangleq \{(a,b) : a,b \in H \land a.rtime < b.stime\}.$
- ss (same-session) is an equivalence relation on H that groups pairs of operations invoked by the same process we say such operations belong to the same session. Formally:  $ss \triangleq \{(a,b) : a,b \in H \land a.proc = b.proc\}$ .
- so (session order) is a partial order defined as:  $so \triangleq rb \cap ss$ .
- ob (same-object) is an equivalence relation on H that groups pairs of operations invoked on the same object. Formally:  $ob \triangleq \{(a,b) : a,b \in H \land a.obj = b.obj\}$ .
- concur as the symmetric binary relation designating all pairs of real-time concurrent operations invoked on the same object. Formally:  $concur \triangleq ob \setminus rb$ .

For  $(a,b) \in rel$  we sometimes alternatively write  $a \xrightarrow{rel} b$ . We further denote by  $rel^{-1}$  the inverse relation of rel. For the sake of a more compact notation, we use binary relation projections. For instance,  $rel|_{wr \to rd}$  identifies all pairs of operations belonging to rel consisting of a write and a read operation. Furthermore, if rel is an equivalence relation, we adopt the notation  $a \approx_{rel} b \triangleq [a \xrightarrow{rel} b]$ . We recall that an equivalence relation rel on set H partitions H into equivalence classes  $[a]_{rel} = \{b \in H : b \approx_{rel} a\}$ . We write  $H/\approx_{rel} b$  to denote the set of equivalence classes determined by rel.

<sup>&</sup>lt;sup>3</sup>For better readability, we implicitly assume relations are parametrized by a history.

We complement the *concur* relation with the function  $Concur : H \to 2^H$  to denote the set of write operations concurrent with a given operation:

$$Concur(a) \triangleq \{b \in H|_{wr} : (a,b) \in concur\}$$
 (1)

Abstract executions. We model system executions using the concept of abstract execution, following Burckhardt [2014]. An abstract execution is a multi-graph A=(H,vis,ar) built on a given history H, which it complements with two relations on elements of H, i.e., vis and ar. Whereas histories describe the observable outcomes of executions, vis and ar, intuitively, capture the non-determinism of the asynchronous environment (e.g., message delivery order), as well as implementation-specific constraints (e.g., conflict-resolution policies). In other words, vis and ar determine the relations between pairs of operations in a history that explain and justify its outcomes. More specifically:

- vis (visibility) is an acyclic natural relation that accounts for the propagation of write operations. Intuitively, a be visible to b (i.e.,  $a \xrightarrow{vis} b$ ) means that the effects of a are visible to the process invoking b (e.g., b may read a value written by a). Two write operations are invisible to each other if they are not ordered by vis.
- *ar* (*arbitration*) is a *total* order on operations of the history that specifies how the system resolves conflicts due to concurrent and invisible operations. In practice, such total order can be achieved in various ways: through the adoption of a distributed timestamping [Lamport 1978] or consensus protocol [Birman et al. 1991; Hadzilacos and Toueg 1994; Lamport 2001], using a centralized serializer, or using a deterministic conflict resolution policy.

Depending on constraints expressed by *vis*, during an execution processes may observe different orderings of write operations, which we call *serializations*.

We further define the *happens-before* order (*hb*) as the transitive closure of the union of *so* and *vis*, denoted by:

$$hb \triangleq (so \cup vis)^+ \tag{2}$$

## 2.3. Replicated data types and return value consistency

Rather than defining the current system state as a set of values held by shared objects, following Burckhardt [2014], we employ a graph abstraction called (operation) *context*, which encodes the information of an abstract execution A, taking a projection on visibility (vis) with respect to a given operation op. Formally, given C as the set of contexts of all operations in a given abstract execution A, we define the context of an operation op as:

$$C = cxt(A, op) \triangleq A|_{op, vis^{-1}(op), vis, ar}$$
(3)

Further, we adopt the concept of replicated data type [Burckhardt 2014] to define the type of shared object implemented in the distributed system (e.g., read/write register, counter, set, queue, etc.). For each replicated data type, a function  $\mathcal F$  specifies the set of intended return values of an operation  $op \in H$  in relation to its context, i.e.,  $\mathcal F(op,cxt(A,op))$ . Using  $\mathcal F$ , we can define return value consistency as:

$$RVal(\mathcal{F}) \triangleq \forall op \in H : op.oval \in \mathcal{F}(op, cxt(A, op))$$
(4)

Essentially, return value consistency is a predicate on abstract executions that guarantees that the return value of any given operation of that execution will belong to the set of its intended return values.

Given operation  $b \in H$  and its context cxt(A, b), we let a = prec(b) be the (unique) latest operation preceding b in ar, such that:  $a.oval \neq \nabla \land a \in H|_{wr} \cap vis^{-1}(b)$ . In other

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words, prec(b) is the last write visible to b according to the ordering specified by ar. If no such preceding operation exists (e.g., if b is the first operation of the execution according to ar), by convention prec(b).ival is a default value equal to  $\bot$ .

In this paper we adopt the read/write register (i.e., read/write storage) as reference replicated data type, which is defined by the following intended return value function:

$$\mathcal{F}_{reg}(op, cxt(A, op)) = prec(op).ival$$
 (5)

Note that, while the focus of this survey is on read/write storage, the consistency predicates defined in this paper take  $\mathcal{F}$  as a parameter, and therefore directly extend to other replicated data types.

## 2.4. Consistency semantics

Following Burckhardt [2014], we define *consistency semantics*, sometimes also called *consistency guarantees*, as conditions on attributes and relations of abstract executions, expressed as first-order logic predicates. We write  $A \models \mathcal{P}$  if the consistency predicate  $\mathcal{P}$  is true for abstract execution A. Hence, defining a consistency model amounts to collecting all the required consistency predicates and then specifying that histories must be justifiable by at least an abstract execution that satisfies them all.

Formally, given history H and  $\mathcal{A}$  as the set of all possible abstract executions on H, we say that history H satisfies some consistency predicates  $\mathcal{P}_1, \dots \mathcal{P}_n$  if it can be extended to some abstract execution that satisfies them all:

$$H \models \mathcal{P}_1 \land \dots \land \mathcal{P}_n \Leftrightarrow \exists A \in \mathcal{A} : \mathcal{H}(A) = H \land A \models \mathcal{P}_1 \land \dots \land \mathcal{P}_n$$
 (6)

In the notation above, given the abstract execution A = (H, vis, ar),  $\mathcal{H}(A)$  denotes H.

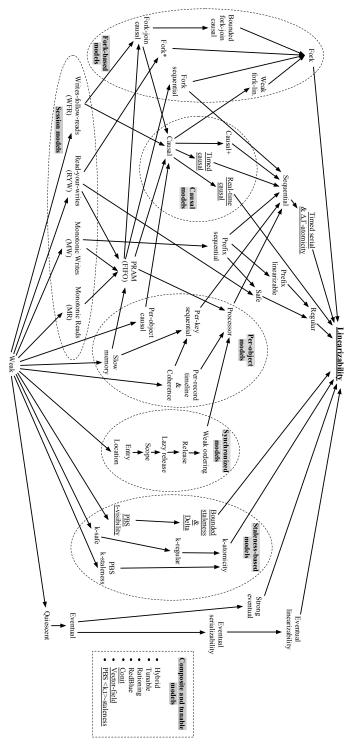
## 3. NON-TRANSACTIONAL CONSISTENCY SEMANTICS

In this section we analyze and survey the consistency semantics of systems which adopt single operations as their primary operational constituent (i.e., non-transactional consistency semantics). The consistency models described in the rest of the paper appear in Figure 1, a comprehensive graph that proposes a partial ordering of consistency semantics according to their semantic strength, as well as a more loosely defined clustering into *families* of consistency models. This classification draws both from strength of different consistency semantics and from the underlying common factors that underpin their definitions.

In the remainder of this section we examine each family of consistency semantics. Section 3.1 introduces linearizability and other strong consistency models, while in Section 3.2 we consider eventual and weak consistency. Next we analyze PRAM and sequential consistency (Section 3.3), and, in Section 3.4, the models based on the concept of session. Section 3.5 proposes an overview of consistency semantics explicitly dealing with causality, while in Section 3.6 we study staleness-based models. This is followed by an overview of fork-based models (Section 3.7). Section 3.8 and 3.9 respectively deal with tunable and per-object semantics. Finally, we survey the family of consistency models based on synchronization primitives (Section 3.10).

## 3.1. Linearizability and related "strong" consistency semantics

The gold standard and the central consistency model for non-transactional systems is **linearizability**, defined by Herlihy and Wing [1990]. Roughly speaking, linearizability is a correctness condition that establishes that each operation shall appear to be applied instantaneously at a certain point in time between its invocation and its response.



 $\label{eq:Fig. 1: Hierarchy of non-transactional consistency models.}$  A directed edge from consistency semantics A to consistency semantics B means that any execution that satisfies B also satisfies A. Underlined models explicitly reason about timing guarantees. ACM Computing Surveys, Vol. V, No. N, Article A, Publication date: January YYYY.

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Linearizability, often informally dubbed *strong consistency*, <sup>4</sup> has been for long regarded as the ideal correctness condition at which distributed storage implementations should aim. Linearizability features a *locality* property: a composition of linearizable objects is itself linearizable – hence, linearizability enables modular design and verification.

Although very intuitive to understand, the strong semantics of linearizability make it challenging to implement. In this regard, Gilbert and Lynch [2002], formally proved the *CAP* theorem, an assertion informally presented in previous works [Johnson and Thomas 1975; Davidson et al. 1985; Coan et al. 1986; Brewer 2000], that binds linearizability to the ability of a system of maintaining a non-trivial level of availability when confronted with network partitions. In a nutshell, the *CAP* theorem states that in presence of network partitions a distributed storage system has to sacrifice either availability or linearizability.

Burckhardt [2014] breaks down linearizability into three components:

$$LINEARIZABILITY(\mathcal{F}) \triangleq SINGLEORDER \land REALTIME \land RVAL(\mathcal{F})$$
 (7)

where:

SINGLEORDER 
$$\triangleq \exists H' \subseteq \{op \in H : op.oval = \nabla\} : vis = ar \setminus (H' \times H)$$
 (8)

and

$$REALTIME \triangleq rb \subseteq ar \tag{9}$$

In other words, SINGLEORDER imposes a single global order that defines both vis and ar, whereas REALTIME constrains arbitration (ar) to comply to the returns-before partial ordering (rb). Finally, RVAL $(\mathcal{F})$  specifies the return value consistency of a replicated data type. We recall that, as per Eq. 5, in case of read/write storage this is the value written by the last write (according to ar) visible to a given read operation rd.

A definition tightly related to that one of linearizability had been previously provided by Lamport [1986b] for the **atomic** register semantic. Lamport describes a single-writer multi-reader (SWMR) shared register to be atomic *iff* each read operation not overlapping a write returns the last value actually written on the register, and the read values are the same as if the operations had been performed sequentially (i.e., without overlapping). Essentially, this definition implies the existence of a point in time (the *linearization point*) at which each operation is actually applied on the shared register.<sup>5</sup> It is easy to show that atomicity and linearizability are equivalent for readwrite registers. However, linearizability is a more general condition designed for generic shared data structures that allow for a broader set of operational semantics than those offered by registers.

Besides atomic registers, Lamport [1986b] defines two slightly weaker semantics for SWMR registers: **safe** and **regular**. In absence of read-write concurrency, they both guarantee that a read returns the last written value, exactly like the atomic semantics. The difference between the three resides in the allowed set of return values for a read operation concurrent with a write. Namely, with a safe register, a read concurrent with some write may return any value. On the other hand, with a regular register, a read operation concurrent with some writes may return either the value written by the most recent complete write, or a value written by a concurrent write. This difference is illustrated in Figure 2.

<sup>&</sup>lt;sup>4</sup>Note that the adjective "strong" has also been used in literature to identify indistinctly *linearizability* and *sequential consistency* (which we define in Section 3.3), as they both entail single-copy-semantics and require that a single ordering of operations be observed by all processes.

<sup>&</sup>lt;sup>5</sup>The existence of an instant at which each operation becomes atomically *visible* had originally been postulated by Lamport [1983].

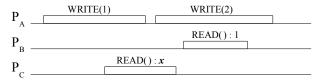


Fig. 2: An execution exhibiting read-write concurrency (real time flows from left to right). The register is initialized to 0. Atomic (linearizable) semantics allow x to be 0 or 1. Regular semantics allow x to be 0, 1 or 2. With safe semantics x may be any value.

Formally, regular and safe semantics can be defined as follows:

$$REGULAR(\mathcal{F}) \triangleq SINGLEORDER \land REALTIMEWRITES \land RVAL(\mathcal{F})$$
(10)

$$SAFE(\mathcal{F}) \triangleq SINGLEORDER \land REALTIMEWRITES \land SEQRVAL(\mathcal{F})$$
(11)

where

REALTIMEWRITES 
$$\triangleq rb|_{wr \to op} \subseteq ar$$
 (12)

is a restriction of real-time ordering only for writes (preceding reads or other writes), and

$$SEQRVAL(\mathcal{F}) \triangleq \forall op \in H : Concur(op) = \emptyset \Rightarrow op.oval \in \mathcal{F}(op, cxt(A, op))$$
 (13)

which restricts the return value consistency only to read operations that are not concurrent with any write.

## 3.2. Weak and eventual consistency

At the opposite end of the consistency spectrum lies **weak** consistency. Although this term has been traditionally used in literature to identify any consistency model weaker than sequential consistency, recent works [Vogels 2008; Bermbach and Kuhlenkamp 2013] associate it to a more specific albeit rather vague definition: a weakly consistent system does not guarantee that reads return the most recent value written, and several (often underspecified) requirements have to be satisfied for a value to be returned. In effect, weak consistency does not provide ordering guarantees – hence, no synchronization protocol is actually required. Even though this model might seem to have limited usability, it is in fact implemented in situations in which having a synchronization protocol would be too costly, and a fortuitous exchange of information between replicas can be good enough. For example, a typical use case for weak consistency are the relaxed caching policies that can be applied across various tiers of a web application, or even the cache implemented in web browsers.

**Eventual** consistency is a slightly stronger notion than weak consistency. Namely, under eventual consistency, replicas converge towards identical copies in the absence of further updates. In other words, if no new write operations are invoked on the object, *eventually* all reads will return the same value. Eventual consistency was first defined by Terry et al. [1994] and then further popularized more than a decade later by Vogels [2008] with the advent of highly available storage systems (i.e., *AP* systems in the CAP theorem parlance). Eventual consistency is especially suited in contexts where coordination is not practical or too expensive (e.g., in mobile and wide area settings) [Saito and Shapiro 2005]. Despite its wide adoption, eventual consistency leaves to the application programmer the burden of dealing with transient *anomalies* – i.e., behaviors deviating from that of an ideal linearizable execution. Hence, a quite large body of recent work has been aiming to achieve a better understanding of its subtle implications [Bermbach and Tai 2011; Bernstein and Das 2013; Bailis and Ghodsi 2013; Bailis et al.

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2014]. At its core, eventual consistency constrains replicas' eventual state (i.e., their *convergence*): in fact it does not provide any guarantees about recency and ordering of operations. Burckhardt [2014] proposes a formal definition of eventual consistency:

EVENTUAL CONSISTENCY  $(\mathcal{F}) \triangleq$ 

Eventual Visibility 
$$\land$$
 NoCircular Causality  $\land$  RVal $(\mathcal{F})$  (14)

where:

EVENTUALVISIBILITY  $\triangleq \forall a \in H, \forall [f] \in H / \approx_{ss}$ :

$$|\{b \in [f] : (a \xrightarrow{rb} b) \land (a \xrightarrow{vis} b)\}| < \infty$$
 (15)

and

$$NoCircularCausality \triangleq acyclic(hb)$$
 (16)

that is, the acyclic projection of hb, defined in Eq. 2. EVENTUALVISIBILITY mandates that, eventually, operation op will be visible to another operation op' invoked after the completion of op.

In an alternative attempt at clarifying the definition of eventual consistency, Shapiro et al. [2011a] identify the following properties from replicas' viewpoint:

- *Eventual delivery*: if some correct replica applies a write operation *op*, *op* is eventually applied by all correct replicas;
- *Convergence*: all correct replicas that have applied the same write operations eventually reach equivalent state;
- Termination: all operations complete.

To this definition of eventual consistency, Shapiro et al. [2011a] add the following constraint:

— *Strong convergence*: all correct replicas that have applied the same write operations *have* equivalent state.

In other words, this last property guarantees that any two replicas that have applied the same (possibly unordered) set of writes will hold the same data. A storage system enforcing both eventual consistency and strong convergence is said to implement **strong eventual** consistency.

We capture strong convergence from the perspective of read operations, by requiring that reads which have the identical sets of visible writes return the same values.

STRONGCONVERGENCE 
$$\triangleq \forall a, b \in H|_{rd} : vis^{-1}(a)|_{wr} = vis^{-1}(b)|_{wr} \Rightarrow a.oval = b.oval$$
 (17)

Then, strong eventual consistency can be defined as:

STRONGEVENTUAL CONSISTENCY  $(\mathcal{F}) \triangleq$ 

Eventual Consistency 
$$(\mathcal{F}) \wedge Strong Convergence$$
 (18)

**Quiescent** consistency [Herlihy and Shavit 2008] requires that if an object stops receiving updates (i.e., becomes quiescent), then the execution is equivalent to some sequential execution containing only complete operations. Although this definition resembles eventual consistency, it does not guarantee termination: a system that does not stop receiving updates will not reach quiescence, thus replicas convergence.

Following [Burckhardt 2014], we formally define quiescent consistency as:

QUIESCENTCONSISTENCY(
$$\mathcal{F}$$
)  $\triangleq |H|_{wr}| < \infty \Rightarrow$   
 $\exists C \in \mathcal{C} : \forall [f] \in H/\approx_{ss} : |\{op \in [f] : op.oval \notin \mathcal{F}(op, C)\}| < \infty$  (19)

#### 3.3. PRAM and sequential consistency

Pipeline RAM (PRAM or FIFO) consistency [Lipton and Sandberg 1988] prescribes that all processes see write operations issued by a given process in the same order as they were invoked by that process. On the other hand, processes may observe writes issued by different processes in different orders. Thus, no global total ordering is required. However, the writes from any given process (session) must be serialized in order, as if they were in a pipeline - hence the name. We define PRAM consistency by requiring the visibility partial order to be a superset of session order:

$$PRAM \triangleq so \subseteq vis \tag{20}$$

As proved by Brzezinski et al. [2003], PRAM consistency is ensured iff the system provides read-your-write, monotonic reads and monotonic writes guarantees, which we will introduce in Section 3.4.

In a storage system implementing sequential consistency all operations are serialized in the same order on all replicas, and the ordering of operations determined by each process is preserved. Formally:

$$SEQUENTIALCONSISTENCY(\mathcal{F}) \triangleq SINGLEORDER \land PRAM \land RVAL(\mathcal{F})$$
(21)

Thus, sequential consistency, first defined in [Lamport 1979], is a guarantee of ordering rather than recency. Like linearizability, sequential consistency enforces a common global order of operations. Unlike linearizability, sequential consistency does not require real-time ordering of operations across different sessions: only the real-time ordering of operations invoked by the same process is preserved (as in PRAM consistency). A quantitative comparison of the power and costs involved in the implementation of sequential consistency and linearizability is presented by Attiya and Welch [1994].



Fig. 3: An execution with processes issuing write operations on a shared object. Black spots are the chosen linearization points.

Figure 3 shows an execution featuring two processes issuing write operations on a shared object. Let us suppose that the two processes also continuously perform read operations. Each process will observe a certain serialization of the write operations. If we were to assume that the system respects PRAM consistency, those two processes might observe, for instance, the following two serializations:

$$S_{P_A}: W1 W2 W3 W5 W4 W7 W6 W8$$
 (S.1)  $S_{P_B}: W1 W3 W5 W7 W2 W4 W6 W8$  (S.2)

$$S_{P_{\rm R}}: W1 W3 W5 W7 W2 W4 W6 W8$$
 (S.2)

If the system implemented sequential consistency, then  $S_{P_A}$  would be equal to  $S_{P_B}$ and it would respect the ordering of operations imposed by each writing process. Thus,

 $<sup>^6</sup>$ In Section 3.10 we present *processor* consistency: a model whose semantic strength stands between those of PRAM and sequential consistency.

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any of (S.1) or (S.2) would be acceptable. On the other hand, assuming the system implements linearizability, and assigning linearization points as indicated by the points in Figure 3, (S.3) would be the only allowed serialization:

$$S_{Lin}: W1 W3 W2 W4 W5 W6 W8 W7$$
 (S.3)

#### 3.4. Session guarantees

Session guarantees were first described by Terry et al. [1994]. Although originally defined in connection to *client* sessions, session guarantees may as well apply to situations in which the concept of session is more loosely defined and it just refers to a specific process' point of view on the execution. We note that previous works in literature have classified session guarantees as client-centric models [Tanenbaum and van Steen 2007].

Monotonic reads states that successive reads must reflect a non-decreasing set of writes. Namely, if a process has read a certain value v from an object, any successive read operation will not return any value written before v. Intuitively, a read operation can be served only by those replicas that have executed all write operations whose effects have already been observed by the requesting process. In effect, we can represent this by saying that, given three operations  $a,b,c\in H$ , if  $a\xrightarrow{\text{vis}}b$  and  $b\xrightarrow{\text{so}}c$ , where b and c are read operations, then  $a \xrightarrow{\text{vis}} c$ , i.e., the transitive closure of vis and so is included

MONOTONICREADS 
$$\triangleq \forall a \in H, \forall b, c \in H|_{rd} : a \xrightarrow{\text{vis}} b \wedge b \xrightarrow{\text{so}} c \Rightarrow a \xrightarrow{\text{vis}} c$$
  
 $\triangleq (vis; so|_{rd \to rd}) \subseteq vis$  (22)

Read-your-writes guarantee (also called read-my-writes [Terry et al. 2013; Burckhardt 2014) requires that a read operation invoked by a process can only be carried out by replicas that have already applied all writes previously invoked by the same process.

READYOURWRITES 
$$\triangleq \forall a \in H|_{wr}, \forall b \in H|_{rd} : a \xrightarrow{so} b \Rightarrow a \xrightarrow{vis} b$$
  
 $\triangleq so|_{wr \to rd} \subseteq vis$  (23)

Let us assume that two processes issue read and write operations on a shared object as in Figure 4.

Fig. 4: An execution with processes issuing read and write operations on a shared object.

Given such execution,  $P_A$  and  $P_B$  could observe the following serializations, which satisfy the read-your-write guarantee but not PRAM consistency:

$$S_{P_A}: W1 W3 W4 W2$$
 (S.4)

$$S_{P_A}: W1 W3 W4 W2$$
 (S.4)  
 $S_{P_B}: W2 W4 W3 W1$  (S.5)

We note that some works in literature refer to session consistency as a special case of read-your-writes consistency that can be attained through sticky client sessions, i.e., those sessions in which the process always invokes operations on a given replica.

In a system that ensures **monotonic writes** a write is only performed on a replica if the replica has already performed all previous writes of the same session. In other

words, replicas shall apply all writes belonging to the same session according to the order in which they were issued.

MONOTONICWRITES 
$$\triangleq \forall a, b \in H|_{wr} : a \xrightarrow{so} b \Rightarrow a \xrightarrow{ar} b \triangleq so|_{wr \to wr} \subseteq ar$$
 (24)

**Writes-follow-reads**, sometimes called *session causality*, is somewhat the converse concept of read-your-write guarantee as it ensures that writes made during the session are ordered after any writes made by any process on any object whose effects were seen by previous reads in the same session.

WRITESFOLLOWREADS 
$$\triangleq \forall a, c \in H|_{wr}, \forall b \in H|_{rd} : a \xrightarrow{\text{vis}} b \wedge b \xrightarrow{\text{so}} c \Rightarrow a \xrightarrow{\text{ar}} c$$
  
 $\triangleq (vis; so|_{rd \to wr}) \subseteq ar$  (25)

We note that some of the session guarantees embed specific notions of causality, and that in fact, as proved by Brzezinski et al. [2004], causal consistency – which we describe next – requires and includes them all.

#### 3.5. Causal models

The commonly accepted notion of potential causality in distributed systems has been enclosed in the definition of the *happened-before* relation introduced by Lamport [1978]. According to this relation, two operations a and b are ordered if (a) they are both part of the same thread of execution, (b) b reads a value written by a, or (c) they are related by a transitive closure leveraging (a) and/or (b). This notion, originally defined in the context of message passing systems, has been translated to a consistency condition for shared-memory systems by Hutto and Ahamad [1990]. The potential causality relation establishes a partial order over operations which we represent as hb in (2). Hence, while operations that are potentially causally related must be seen by all processes in the same order, operations that are not causally related (i.e., causally concurrent) may be observed in different orders by different processes. In other words, **causal** consistency dictates that all replicas agree on the ordering of causally related operations [Hutto and Ahamad 1990; Ahamad et al. 1995; Mahajan et al. 2011]. This can be expressed as the conjunction of two predicates [Burckhardt 2014]:

- CAUSALVISIBILITY  $\triangleq hb \subseteq vis$ — CAUSALARBITRATION  $\triangleq hb \subseteq ar$
- Hence, causal consistency is defined as:

$$CAUSALITY(\mathcal{F}) \triangleq CAUSALVISIBILITY \wedge CAUSALARBITRATION \wedge RVAL(\mathcal{F})$$
 (26)

Figure 5 represents an execution with two processes writing and reading the value of a shared object, with arrows indicating the causal relationships between operations.

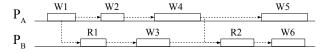


Fig. 5: An execution with processes issuing operations on a shared object.

Arrows express causal relationships between operations.

 $<sup>^{7}</sup>$ While the most appropriate terminology would be "potential causality", for simplicity, hereafter we will use "causality".

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Assuming the execution respects PRAM but not causal consistency, we might have the following serializations:

$$S_{P_A}: W1 W2 W4 W5 W3 W6$$
 (S.6)

$$S_{P_{R}}: W3 \ W6 \ W1 \ W2 \ W4 \ W5$$
 (S.7)

Otherwise, with causal consistency (which implies PRAM), we could have obtained these serializations:

$$S_{P_A}: W1 W3 W2 W4 W5 W6$$
 (S.8)

$$S_{P_R}: W1 W2 W3 W4 W6 W5$$
 (S.9)

Recent work by Bailis et al. [2012] promotes the use of explicit application-level causality, which is a subset of potential causality,<sup>8</sup> for building highly available distributed systems that would entail less overhead in terms of coordination and metadata maintenance. Furthermore, an increasing body of research has been drawing attention on causal consistency, considered as an optimal tradeoff between user-perceived correctness and coordination overhead, especially in mobile or geo-replicated applications [Lloyd et al. 2011; Bailis et al. 2013; Zawirski et al. 2015].

Causal+ (or convergent causal) consistency [Lloyd et al. 2011] mandates, in addition to causal consistency, that all replicas should eventually and independently agree on conflicts resolution. In fact, causally concurrent write operations may generate conflicting outcomes which in convergent causal consistent systems are handled in the same way by commutative and associative functions. Essentially, causal+ strengthens causal consistency with strong convergence (see Equation (17)), which mandates that all correct replicas that have applied the same write operations have equivalent state. In a sense, causal+ consistency augments causal consistency with strong convergence, in the vein strong eventual consistency [Shapiro et al. 2011a] strengthens eventual consistency. Hence, causal+ consistency can be expressed as:

$$Causal+(\mathcal{F}) \triangleq Causality(\mathcal{F}) \land StrongConvergence$$
 (27)

**Real-time causal** consistency has been defined in [Mahajan et al. 2011] as a stricter condition than causal consistency that enforces an additional condition: causally concurrent write operations that do not overlap in real-time must be applied according to their real-time order.

$$REALTIMECAUSALITY(\mathcal{F}) \triangleq CAUSALITY(\mathcal{F}) \land REALTIME$$
 (28)

where REALTIME is defined as in (9).

We note that although [Lloyd et al. 2011] classifies real-time causal consistency as stronger than causal+ consistency, they are actually incomparable, as real-time causality — as defined in [Mahajan et al. 2011] — does not imply strong convergence. Of course, one can devise a variant of real-time causality that respects strong convergence as well.

Attiya et al. [2015] define *observable causal* consistency as a strengthening of causal consistency for multi-value registers (MVR) that enforces the exposure of concurrency between operations when this concurrency may be inferred by processes from their observations. Observable causal consistency has also been proved to be the strongest consistency model satisfiable for a certain class of highly-available data stores implementing MVRs.

<sup>&</sup>lt;sup>8</sup>As argued in [Bailis et al. 2012], the application-level causality graph would be smaller in fanout and depth with respect to the traditional causal one, because it would only enclose relevant causal relationships, hinging on application-level knowledge and user-facing outcomes.

#### 3.6. Staleness-based models

Intuitively, staleness based models allow reads to return old, *stale* written values. They provide stronger guarantees than eventually consistent semantics, but weak enough to allow for more efficient implementations than linearizability. In literature, two common metrics are employed to measure staleness: (real) time and data (object) versions.

To the best of our knowledge, the first formalization of a consistency model explicitly dealing with time-based staleness is proposed by Singla et al. [1997] as **delta** consistency. According to delta consistency, writes are guaranteed to become visible at most after t + delta time units. Moreover, delta consistency is defined in conjunction with an ordering criterion (which is reminiscent of the *slow memory* consistency model, that we postpone to Section 3.9): writes to a given object by the same process are observed in the same order by all processes, but no global ordering is enforced for writes to a given object by different processes.

In an analogous way, *timed consistency* models, as defined by Torres-Rojas et al. [1999], restrict the sets of values that read operations may return by the amount of time elapsed since the preceding writes. Specifically, in a *timed serialization* all reads occur on time, i.e., they do not return stale values when there are more recent ones that have been available for more than  $\Delta$  units of time –  $\Delta$  being a parameter of the execution. In other words, similarly to delta consistency, if a write operation is performed at time t, the value written by this operation must be visible by all processes by time  $t + \Delta$ .

Mahajan et al. [2010] define a consistency condition named **bounded staleness** which at its core is very similar to that of timed and delta semantics: a write operation of a given process becomes visible to other processes no later than a fixed amount of time. However, this definition is also related to the use of a periodic message (i.e., a *beacon*) which allows each process to keep up with updates from other processes or *suspect* of missing updates.

The differences among delta consistency, timed reads and bounded staleness are in fact matter of subtle operational details that derive from the diverse contexts and practical purposes for which those models were developed. Hence, we can describe in formal terms the core semantics expressed by delta consistency, timed consistency models and bounded staleness as the following condition:

 $\mathbf{TimedVisibility}(\Delta) \triangleq \forall a \in H|_{wr}, \forall b \in H, \forall t \in \mathit{Time}:$ 

$$a.rtime = t \wedge b.stime = t + \Delta \Rightarrow a \xrightarrow{\text{vis}} b$$
 (29)

**Timed causal** consistency [Torres-Rojas and Meneses 2005] guarantees that each execution respects the partial ordering of causal consistency and that all reads are *on time*, with tolerance  $\Delta$ :

$$TIMEDCAUSALITY(\mathcal{F}, \Delta) \triangleq CAUSALITY(\mathcal{F}) \wedge TIMEDVISIBILITY(\Delta)$$
 (30)

As depicted in Figure 1, due to the timed visibility term, timed causal is a semantic condition stronger than causal consistency.

Similarly, **timed serial** consistency [Torres-Rojas and Meneses 2005] combines the real-time global ordering guarantee with the timed serialization constraint. Hence, a timed serial consistent execution with  $\Delta=0$  would in fact be linearizable.

Golab et al. [2011] describe  $\Delta$ -atomicity, a semantic condition which is in fact equivalent to timed serial consistency. Namely, according to  $\Delta$ -atomicity read operations may return either the value written by the last preceding write, or the value of a write operation returned up to  $\Delta$  time units ago. In a follow-up work [Golab et al. 2014], the same authors propose a novel metric called  $\Gamma$  which entails fewer assumptions and is more robust than  $\Delta$  against clock skews. The corresponding consistency semantics,

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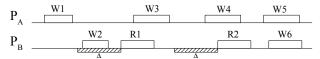
 $\Gamma$ -atomicity, expresses, as  $\Delta$ -atomicity, a "deviation" in time of a given execution from a linearizable one having the same operations' outcomes.

We express the core notion of  $\Delta$ -atomicity,  $\Gamma$ -atomicity and timed serial consistency in the following predicate:

TIMEDLINEARIZABILITY( $\mathcal{F}, \Delta$ )  $\triangleq$ 

SINGLEORDER 
$$\land$$
 TIMEDVISIBILITY( $\triangle$ )  $\land$  RVAL( $\mathcal{F}$ ) (31)

Figure 6 illustrates an execution featuring read operations of which outcomes should depend on a fixed timing parameter  $\Delta$ .



*Fig.* 6: An execution with processes issuing operations on a shared object. Hatched rectangles highlight the  $\Delta$  parameter of staleness-based read operations.

If we were to assume that, despite the timing parameter,  $P_A$  and  $P_B$  observed the following serialization:

$$S_{P_{A,B}}: W2 W6 W1 W3 W4 W5$$
 (S.10)

then such execution would be sequentially consistent but it would not satisfy timed serial consistency requirements. Thus, this execution serves as hint of the relative strengths of sequential and timed serial consistency models as represented in Fig. 1.

**Prefix** consistency [Terry et al. 1995; Terry 2013], also dubbed **timeline** consistency [Cooper et al. 2008], grants readers the guarantee of observing an ordered sequence of writes which nonetheless may not contain the most recent ones. So it expresses a constraint in matter of ordering rather than recency of writes: the read value is the result of a specific sequence of writes upon whose order all replicas have agreed. This pre-established order is supposedly reminiscent of that one imposed by sequential consistency. Thus, we could rename prefix consistency as *prefix sequential* consistency, whereas a version abiding real-time constraints would be called *prefix linearizable* consistency. Formally, we describe prefix sequential consistency as:

$$PREFIXSEQUENTIAL(\mathcal{F}) \triangleq SINGLEORDER \land MONOTONICWRITES \land RVAL(\mathcal{F}) \quad (32)$$

where the term named MONOTONICWRITES implies that the ordering of writes belonging to the same session is respected, as defined in (24). Similarly, we express prefix linearizable consistency as:

 $PREFIXLINEARIZABLE(\mathcal{F}) \triangleq SINGLEORDER \land REALTIMEWW \land RVAL(\mathcal{F})$  (33)

where

$$REALTIMEWW \triangleq rb|_{wr \to wr} \subseteq ar \tag{34}$$

In a study on quorum-based replicated systems with malicious faults, Aiyer et al. [2005] formalize relaxed semantics that tolerate limited version-based staleness. Substantially, *K*-safe, *K*-regular and *K*-atomic (or *K*-linearizability) generalize the register consistency conditions previously introduced in [Lamport 1986a] and described

in Section 3.1, by permitting reads non-overlapping concurrent writes to return one of the latest K values written. For instance K-linearizability can be formalized as:

$$K$$
-LINEARIZABLE $(\mathcal{F}, K) \triangleq$ 

SINGLEORDER 
$$\land$$
 REALTIMEWW  $\land$  K-REALTIMEREADS $(K) \land$  RVAL $(\mathcal{F})$  (35)

where

K-RealTimeReads
$$(K) \triangleq \forall a \in H|_{wr}, \forall b \in H|_{rd}, \forall PW \subseteq H|_{wr}, \forall pw \in PW:$$

$$|PW| < K \land a \xrightarrow{ar} pw \land pw \xrightarrow{rb} b \land a \xrightarrow{rb} b \Rightarrow a \xrightarrow{ar} b \quad \textbf{(36)}$$

Finally, Bailis et al. [2012] build on these results a series of probabilistic models to predict the staleness of reads performed on eventually consistent quorum-based stores. They provide definitions of Probabilistically Bounded Staleness (PBS) k-staleness and PBS t-visibility. While the first describes a probabilistic model which restricts the staleness of values returned by read operations, the latter limits probabilistically the time before a write becomes visible. The combination of these two models is named PBS  $\langle k, t \rangle$ -staleness. In a sense, PBS k-staleness is a probabilistic weakening of K-atomicity, i.e., the one that with probability equal to 1 becomes K-linearizability. Similarly, PBS t-visibility is a probabilistic weakening of timed visibility.

#### 3.7. Fork-based models

Inherent trust limitations that arise in the context of outsourced storage and computations [Cachin et al. 2009b; Vukolić 2010] has revamped the research on algorithms and protocols expressly conceived to deal with Byzantine faults [Lamport et al. 1982], i.e faults that encompass arbitrary and malicious behavior. In the Byzantine fault model, faulty processes and shared objects may tamper data (within the limits of cryptography) or perform other arbitrary operations in order to deliberately disrupt executions.

Together with these algorithms, new consistency models were defined that reshaped the correctness conditions in accordance to what is actually attainable when coping with such strong fault assumptions. Whereas in the context of several untrusted storage repositories Byzantine fault tolerance could be applied to mask certain fault patterns [Vukolić 2010; Bessani et al. 2013] and even implement strong consistency semantics (e.g., linearizability) [Bessani et al. 2014; Dobre et al. 2014], when dealing with a single untrusted storage repository, the situation is different and the consistency needs to be relaxed [Cachin et al. 2009b]. Feasible consistency semantics in the context of interactions of correct clients with untrusted (Byzantine) storage have been captured within the family of fork-based consistency models. In a nutshell, systems dealing with untrusted storage aim at providing linearizability when the storage is correct, but (gracefully) degrade to weaker consistency models, specifically, fork-based consistency models, when the storage exhibits a Byzantine fault.

The forefather of this family of models is **fork** (or fork-linearizable) consistency, introduced by Mazières and Shasha [2002]. In short, a fork-linearizable system guarantees that if the storage system causes the visible histories of two processes to differ even for just a single operation, they may never again observe each other's writes after that without the server being exposed as faulty. Specifically, any divergence in the histories observed by different groups of correct processes can be easily spotted by using any available communication protocol between them (e.g., out-of-band communication, gossip protocols, etc.). Fork-linearizability respects session order (PRAM semantics)

<sup>&</sup>lt;sup>9</sup>Strictly speaking, K-linearizability implicitly assumes K initial writes (i.e., writes with input value  $\bot$ ) [Aiyer et al. 2005].

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and real-time arbitration, thus can be expressed as follows:

$$FORKLINEARIZABILITY(\mathcal{F}) \triangleq PRAM \land REALTIME \land NOJOIN \land RVAL(\mathcal{F})$$
(37)

where the NoJoin predicate stipulates that clients whose sequences of visible operations (also called *views*) have been forked by an adversary, cannot be joined again:

NoJoin 
$$\triangleq \forall a_i, b_i, a_j, b_j \in H : a_i \not\approx_{ss} a_j \land (a_i, a_j) \in ar \setminus vis \land a_i \preceq_{so} b_i \land a_j \preceq_{so} b_j$$
  
 $\Rightarrow (b_i, b_j), (b_j, b_i) \notin vis$  (38)

A subsequent model named **fork\*** consistency was defined in [Li and Mazières 2007] in order to allow the design of protocols that would offer better performance and liveness guarantees. Fork\* consistency relaxes the conditions of fork consistency by allowing forked groups of processes to observe at most one common operation issued by a certain correct process.

 $Fork*(\mathcal{F}) \triangleq ReadYourWrites \land RealTime \land AtMostOneJoin \land RVal(\mathcal{F}) \ \ \textbf{(39)}$  where

ATMOSTONEJOIN 
$$\triangleq \forall a_i, a_j \in H : a_i \not\approx_{ss} a_j \land (a_i, a_j) \in ar \setminus vis \Rightarrow$$

$$\land |\{b_i \in H : a_i \preceq_{so} b_i \land (\exists b_j \in H : a_j \preceq_{so} b_j \land b_i \xrightarrow{vis} b_j\}| \leq 1 \quad \textbf{(40)}$$

$$\land |\{b_i \in H : a_i \preceq_{so} b_i \land (\exists b_i \in H : a_i \preceq_{so} b_i \land b_i \xrightarrow{vis} b_i\}| \leq 1$$

Notice that, unlike fork-linearizability, fork\* does not respect monotonicity of reads (and hence PRAM) [Cachin et al. 2011].

**Fork-sequential** consistency [Oprea and Reiter 2006; Cachin et al. 2009a] requires that whenever an operation becomes visible to multiple processes, all these processes share the same history of operations occurring before that operation. Therefore, whenever a process reads a certain value written by another process, the reader is guaranteed to share with the writer process the set of visible operation that precede that write operation. Essentially, similarly to sequential consistency, a global order of operations is ensured up to a common visible operation. Formally:

$$FORKSEQUENTIAL(\mathcal{F}) \triangleq PRAM \land NoJoin \land RVAL(\mathcal{F})$$
(41)

Mahajan et al. define **fork-join causal** consistency (FJC) as a weaker variant of causal consistency that can preserve safeness and availability in spite of Byzantine faults [Mahajan et al. 2010]. In a fork-join causal consistent storage system if a write operation op issued by a correct process depends on a write operation op' issued by any process, then, at every correct process, op' becomes visible before op. In other words, FJC enforces causal consistency among correct processes. Besides, partitioned groups of processes are allowed to reconcile their histories through merging policies, since inconsistent writes by a Byzantine process are treated as concurrent writes by multiple *virtual processes*. **Bounded fork-join causal** [Mahajan et al. 2011] refines this clause by limiting the number of forks accepted from a faulty node and thus bounding the number of virtual nodes needed to represent each faulty node.

Finally, **weak fork-linearizability** [Cachin et al. 2011] relaxes fork-linearizability conditions in two ways: (1) after being partitioned in different groups, two processes may share the visibility of one more operation (i.e., *at-most-one-join*, as in fork\* consistency) and (2) the real-time order of the last visible operation by each process may not be preserved (i.e., *weak real-time order*). These two conditions enable the design of protocols that allow for improved liveness guarantees (i.e., *wait freedom*). Weak

fork-linearizability can be expressed as:

 $WeakForkLin(\mathcal{F}) \triangleq PRAM \wedge K-RealTime(2) \wedge ATMOSTONEJOIN \wedge RVAL(\mathcal{F})$ (42)

where K-REALTIME(2) predicate is equivalent K-REALTIMEREADS(2) defined in Equation 36, when generalized to all operations (i.e., when the predicate holds  $\forall op \in H$ ). We note that weak fork-linearizability and fork\* consistency are incomparable [Cachin et al. 2011].

## 3.8. Composite and tunable semantics

To bridge the gap between strongly consistent and efficient implementations, several works have proposed consistency models that entail the use of different semantics in an adaptive fashion according to the contingent tradeoffs of performance and correctness. <sup>10</sup>

The idea of distinguishing operations' consistency requirements by their semantics dates back to the shared-memory systems era. In that context, consistency models that employed different ordering constraints depending on operations' types (e.g., *acquire* and *release*, rather than read/write data accesses) were called *hybrid*, whereas those that did not operate distinctions were referred to as *uniform* [Mosberger 1993; Dubois et al. 1986; Gharachorloo et al. 1990].

A first formal definition which presents a similar diversification was proposed by Attiya and Friedman [1992] for shared-memory multiprocessors. **Hybrid** consistency is defined as a model requiring a concerted adoption of weak and strong consistency semantics. In a hybrid consistent system *strong* operations are guaranteed to be seen in some sequential order by all processes (as in sequential consistency), while *weak* operations are designed to be fast, and they eventually become visible by all processes (much like in eventual consistency). Weak operations are only guaranteed to be ordered according to their interleaving with strong operations: if two operations belong to the same session and one of them is strong, then their relative order of invocation is respected and visible by all processes.

In a similar manner, Ladin et al. [1992] tackle the tradeoff between performance and consistency by assigning to each operation an ordering type. *Causal* operations respect causality ordering among them, *forced* operations are delivered in the same order at all relicas, and *immediate* operations are performed as they return and they are delivered by each replica in same order with respect to all other operations.

**Eventual serializability**<sup>11</sup> is described in [Fekete et al. 1996] as a condition that requires a partial ordering of operations which eventually settle to a total order. According to this model, operations might be *strict* or *non-strict*. Strict operations are required to be *stable* as soon as they obtain a response, while non-strict ones may be reordered afterwards. An operation is said to be *stable* if the prefix of operations preceding it reached a final total order. Fekete et al. [1996] envision an implementation in which processes issue operations attaching to them both the list of identifiers of operations that must be ordered before the requested operation, and a flag that indicates the type of operation (i.e., strict or non-strict). The final global and total order achieved by operations can be regarded as a sequential consistency ordering as no real-time notion is involved.

Similarly, Serafini et al. [2010], distinguish *strong* and *weak* operations. While strong operations are immediately linearized, weak ones are linearized only eventually. Weak operations are thus said to respect **eventual linearizability**. Weak operations are in

<sup>&</sup>lt;sup>10</sup>We do not formulate formal definitions for tunable semantics considering that they can be expressed by combining the logical predicates reported in the rest of the paper.

<sup>&</sup>lt;sup>11</sup>We remark that despite the affinity of its name with those of popular transactional consistency models, eventual serializability has been conceived for non-transactional storage systems.

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fact designed to terminate despite failures, and can therefore violate linearizability for a finite period of time. Essentially, eventual linearizability mandates that operations must be ordered according to their real-time ordering, yet this applies only to operations invoked after a certain time t. Therefore, earlier operations may have observed inconsistent histories and can be temporarily ordered in an arbitrary manner. Ultimately, the operations in a system that implements eventual linearizability gravitate towards a total order that satisfies real-time constraints.

Krishnamurthy et al. [2002] propose a QoS model that allows client applications of a distributed storage system to express their consistency requirements. According to their requirements, clients are then directed by a middleware towards a specific group of replicas implementing synchronous or lazy replication schemes, thus applying strong or weak consistency semantics. This framework is said to provide **tunable** consistency.

In the same vein, Li et al. [2012] propose **RedBlue** consistency. With RedBlue consistency operations are flagged as *blue* or *red* depending on several conditions such as their commutativity and the respect of invariants. According to such classification, operations are then executed locally and replicated in an eventually consistent manner, or serialized with respect to each other through synchronous coordination. In a follow-up work, Li et al. [2014] implement and evaluate a system that would relieve the programmer from having to choose the right consistency level for each operation by exploiting a combination of automatic static and dynamic code analysis.

Yu and Vahdat [2002] propose a continuous consistency spectrum based on three metrics: *staleness*, *order error* and *numerical error*. Those metrics are embedded in a **conit** (portmanteau of "consistency unit"), which is a three-dimensional vector that quantifies the divergence from an ideal linearizable execution. Numerical error accounts for the number of write operations that are already globally applied but not yet propagated to a given replica of a certain object. Order error quantifies the number of writes at any replica that are subject to reordering, while staleness bounds the real-time delay of writes propagation among replicas. Those metrics are an attempt to capture the semantics of some fundamental dimensions of consistency, notably those related to the general requirements of agreement on state and update ordering. Note that, according to this model, and unlike timed consistency (see Section 3.6), time-based staleness is defined from the replicas' viewpoint rather than with respect to the timing of individual operations.

Similarly, Santos et al. [2007] aim at quantifying the divergence of data object replicas by using a three-dimensional consistency vector. Originally designed for distributed multiplayer games on ad-hoc networks, **vector-field** consistency mandates for each object a vector  $\kappa = [\theta, \sigma, \nu]$  that bounds its staleness in a particular *view* of the virtual world. In particular, the vector establishes the maximum divergence of replicas in time  $(\theta)$ , number of updates  $(\sigma)$ , and object value  $(\nu)$ . Unlike conit, this model brings about a notion of locality-awareness as it describes consistency as a vector field deployed throughout the gaming virtual environment.

Later works put forward tunable consistency as a suitable model for cloud storage, since it would enables more flexible quality of service (QoS) policies and service-level agreements (SLAs). Kraska et al. [2009] envision consistency **rationing**, which would entail adapting the consistency level at runtime by taking into account economic concerns. Similarly, Chihoub et al. [2012] explore the possibility of a self-adaptive protocol that dynamically adjusts consistency to meet the application needs. In a sequent work, Chihoub et al. [2013] add the monetary cost to the equation and study its tradeoffs with consistency in cloud settings. Terry et al. [2013] advocate the use of declarative consistency-based SLAs that would allow users of cloud key-value stores to attain a better awareness of the inherent performance-correctness tensions. This

approach has been subsequently implemented as a declarative programming model for tunable consistency by Sivaramakrishnan et al. [2015].

In another attempt at providing stronger consistency semantics for geo-replicated storage, Balegas et al. [2015] introduce *explicit* consistency. Besides providing eventual consistency, a replicated store implementing explicit consistency ensures that application-specific correctness rules (i.e., *invariants*) be respected during executions. In a follow-up work, Gotsman et al. [2016] propose a proof rule to help programmers in the task of assigning fine-grained restrictions on operations in order to respect data integrity invariants.

Finally, in the context of combining different consistency models, it is worth also mentioning systems that turn eventual consistency of data (provided by modern commodity cloud storage services) into linearizability, by relying on comparably small volumes of metadata stored separately from data in linearizable storage. In independent efforts, this technique was recently proposed under the names of *consistency anchor* [Bessani et al. 2014] and *consistency hardening* [Dobre et al. 2014].

## 3.9. Per-object semantics

Per-object (or per-key) semantics have been defined to express consistency constraints on a per-object basis. Intuitively, per-object ordering semantics allow for more efficient implementations than global ordering semantics, i.e., across invocations on all objects, taking advantage of techniques such as sharding and state partitioning.

**Slow memory**, defined by Hutto and Ahamad [1990], is a weaker variant of PRAM consistency. A shared-memory system implementing this condition requires that all processes see the writes of a given process to a given object in the same order. In other words, slow memory delineates a per-object weakening of PRAM consistency:

$$PEROBJECTPRAM \triangleq (so \cap ob) \subseteq vis$$
 (43)

An important concept in this family of semantics is that of **coherence** [Gharachorloo et al. 1990] (or cache consistency [Goodman 1989]) which was first introduced as correctness condition of memory hierarchies in shared-memory multiprocessor systems [Dubois et al. 1986]. Coherence ensures that what has been written to a specific memory location becomes visible in some sequential order by all processors, possibly through their local caches. In other words, coherence requires operations to be globally ordered on a per-object basis. A very similar notion has been coined in recent works [Cooper et al. 2008; Lloyd et al. 2011] as **per-record timeline** consistency. This condition, described in relation to replicated storage, ensures that for each individual key (or object), all processes observe the same ordering of operations. Formally, we capture such condition with the following predicate:

PEROBJECTSINGLEORDER ≜

$$\exists H' \subseteq \{op \in H : op.oval = \nabla\} : ar \cap ob = vis \cap ob \setminus (H' \times H) \quad \textbf{(44)}$$

Moreover, a system in which executions respect ordering of operations by a certain process on each object and a global ordering of all operations invoked on each object, would implement a semantic condition that we could name as *per-object sequential* consistency:

 $PEROBJECTSEQUENTIAL(\mathcal{F}) \triangleq$ 

PEROBJECTSINGLEORDER 
$$\land$$
 PEROBJECTPRAM  $\land$  RVAL $(\mathcal{F})$  (45)

**Processor** consistency, defined by Goodman [1989] and formalized by Ahamad et al. [1993], is expressed by two conditions: (a) writes issued by a process must be observed

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in the order in which they were issued, and (b) if there are two write operations to the same object, all processes observe these operations in the same order. Evidently, the two conditions just mentioned are in fact PRAM and per-record timeline consistency, thus:

$$PROCESSORCONSISTENCY(\mathcal{F}) \triangleq PEROBJECTSINGLEORDER \land PRAM \land RVAL(\mathcal{F}) \tag{46}$$

In addition, few works in literature (e.g., [Moraru et al. 2013]) mention *per-object linearizability*, which is in fact equivalent to linearizability on a per-object basis, due to its *locality* property [Herlihy and Wing 1990].

We further note that one could compose other arbitrary consistency models by refining some of the predicates mentioned in this work to match only operations performed on individual objects. As a case in point, Burckhardt et al. [2014] describe **per-object causal** consistency as a restriction of causal consistency on a per-object basis, which leverages the *per-object happens-before* order, defined as:  $hbo \triangleq ((so \cap ob) \cup vis)^+$ .

### 3.10. Synchronized models

For completeness, in this section we overview semantic conditions defined in the '80s and early '90s in order to model the correctness of multiprocessor shared-memory systems. In order to exploit the computational parallelism of these systems, and, at the same time, to cope with the different performance of the various components (e.g., memories, interconnections, processors, etc.), buffering and caching layers were adopted. Consequently, the fundamental challenge of this kind of architecture is making sure that all memories reflect a common, consistent view of shared data. Thus, system designers employed synchronization variables, i.e., special shared objects that only expose two operations, named acquire and release. The synchronization variables are used as a generic abstraction for implementing logical fences meant to control concurrent accesses to shared data objects. In other words, synchronization variables protect the access to shared data through the implementation of mutual exclusion by means of low level primitives (e.g., locks) or high-level language constructs (e.g., critical sections). While the burden of using such tools is left to the programmer, the system is supposed to distinguish the accesses to shared data from those to the synchronization variables, possibly by implementing and exposing specific low level instructions.

Sequential consistency [Lamport 1979] (which we defined in Section 3.3) was initially adopted as ideal correctness condition for multiprocessors shared-memory systems. Weak ordering<sup>12</sup> as described by Dubois et al. [1986] represents a convenient weakening of sequential consistency that brings about performance improvements. In a system that implements weak ordering: (a) all accesses to synchronization variables must be strongly ordered, (b) no access to a synchronization variable is allowed before all previous reads have been completed, and (c) processes cannot perform reads before issuing an access to a synchronization variable. In particular, Dubois et al. [1986] define operations as strongly ordered if they comply with two specific criteria that constrain the ordering of operations according to their session ordering and relatively to some special instructions supported by pipelined cache-based systems. Weak ordering has been subsequently redefined in terms of coordination requirements between software and hardware. Namely, Adve and Hill [1990] define a synchronization model as a set of constraints on memory accesses that specify how and when synchronization needs to be enforced. Given this definition, "a hardware is weakly ordered with respect to a given synchronization model if and only if it appears sequentially consistent to all software that obey the synchronization model".

 $<sup>^{12}</sup>$ Some works in literature refer to weak ordering as to "weak consistency". We chose to avoid this equivocation by adopting its original nomenclature.

Release consistency, presented by Gharachorloo et al. [1990], is a weaker extension of weak ordering that exploits further detailed information about synchronization operations (i.e., acquire and release) and non-synchronization accesses. Operations have to be labelled before execution by the programmer (or the compiler) as strong or weak. Hence, this widens the classification operated by weak ordering, which included just synchronization and non-synchronization labels. Similarly to hybrid consistency (see Section 3.8), strong operations are ordered according to processor or sequential consistency, whereas the ordering of weak operations is just restricted by the relative ordering with respect to the strong operations invoked by the same process.

Subsequently, several algorithms that slightly alter the original implementation of release consistency have been designed. For instance, **lazy release** consistency [Keleher et al. 1992] is a relaxed implementation of release consistency in which actions that enforce consistency are postponed from the release to the next acquire operation. The rationale of lazy release consistency is reducing the number of messages and the amount of data exchanged in a distributed shared-memory system implemented in software. On the same line, the protocol called *automatic update release consistency* [Iftode et al. 1996a] aims at improving performance substantially over software-only implementation of lazy release consistency, by using an automatic update mechanism provided by a virtual memory mapped network interface.

Bershad and Zekauskas [1991] define **entry** consistency by strengthening the relation between synchronization objects and the data which they guard. According to entry consistency, every object has to be guarded by a synchronization variable. Thus, in a sense, this model is a location-relative weakening of a consistency semantic, similarly to the models surveyed in Section 3.9. Moreover, entry consistency operates a further distinction of the synchronization operations in exclusive and non-exclusive. Thanks to these features, reads can occur with a greater degree of concurrency, thus enabling better performance.

**Scope** consistency [Iftode et al. 1996b] claims to offer most of the potential performance advantages of entry consistency, without requiring explicit binding of data to synchronization variables. The key intuition of scope consistency is the use of an abstraction called *scope* to implicitly capture the relationship between data and synchronization operations. Consistency scopes can be derived automatically from the use of synchronization variables in the program, thus easing the work of programmers.

With the definition of **location** consistency, Gao and Sarkar [2000] forwent the basic assumption of *memory coherence* [Gharachorloo et al. 1990], i.e., the property that ensures that all writes to the same object are observed in the same order by all processes (see Section 3.9). Thus, they explored the possibility of executing multithreaded programs in a correct manner by just exploiting a partial order on writes to shared data. Similarly to entry consistency, in location consistency each object is associated to a synchronization variable. However, thanks to the relaxed undelying ordering constraint, Gao and Sarkar [2000] prove that location consistency can be more efficient and equivalently strong when it is applied to settings with low data contention between processes.

## 4. RELATED WORK

Several works in literature have provided overviews on consistency models. In this section we classify these works according to their different perspectives.

Shared-memory systems. Gharachorloo et al. [1990] proposed a classification of shared memory access policies, specifically regarding their concurrency control semantics (e.g., synchronization operations versus read/write accesses). Mosberger [1993] adopted this classification to conduct a study on the memory consistency models popular at that

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time and their implementation tradeoffs. Adve and Gharachorloo [1996] summarized in a practical tutorial the informal definitions and related issues of consistency models most commonly adopted in shared-memory multiprocessor systems.

Several subsequent works developed uniform frameworks and notations to represent consistency semantics defined in literature [Adve and Hill 1993; Raynal and Schiper 1997; Bataller and Bernabéu-Aubán 1997]. Most notably, Steinke and Nutt [2004] provide a unified theory of consistency models for shared memory systems based on the composition of few fundamental declarative properties. In turn, this declarative and compositional approach outlines a partial ordering over consistency semantics. Similarly, a treatment of composability of consistency conditions had been carried out in [Friedman et al. 2003].

While all these works proved to be valuable and formally sound, they represent only a limited portion of the consistency semantics relevant to modern non-transactional storage systems.

Distributed storage systems. In more recent years, researchers have been proposing categorizations of the most influential consistency models for modern storage systems. Namely, Tanenbaum and van Steen [2007] proposed the client-centric versus data-centric classification, while Bermbach and Kuhlenkamp [2013], expanded such classification and provided descriptions for the most popular models. While practical and instrumental in attaining a good understanding of the consistency spectrum, these works propose informal treatments based on a simple dichotomous categorization which falls short of capturing some important consistency semantics. With this survey we aim at improving over these works, as we adopt a formal model based on first-order logic predicates and graph theory. We derived this model from the one proposed in [Burckhardt 2014], which we modified and expanded in order to enable the definition of a wider and richer range of consistency semantics. Moreover, whereas Burckhardt [2014] focuses mostly on session and eventual semantics, we cover a broader ground including more than 50 different consistency semantics.

Measuring consistency. A concurrent research trend has been straining to design uniform and rigorous frameworks to measure consistency in both shared memory systems and, more recently, in distributed storage systems. Namely, while some works have proposed metrics to assess consistency [Yu and Vahdat 2002; Golab et al. 2014], others have devised methods to verify, given an execution, whether it satisfies a certain consistency model [Misra 1986; Gibbons and Korach 1997; Anderson et al. 2010]. Finally, due to the loose definitions and opaque implementations of eventual consistency, recent research has tried to quantify its inherent anomalies as perceived from a client-side perspective [Wada et al. 2011; Patil et al. 2011; Bermbach and Tai 2011; Rahman et al. 2012; Lu et al. 2015]. In this regard, our work provides a more comprehensive and structured overview of the metrics that can be adopted to evaluate consistency.

Transactional systems. Readers interested in pursuing a formal treatment of the most important consistency models for transactional storage systems may refer to [Adya 1999]. Similarly, other works by Harris et al. [2010] and by Dziuma et al. [2014] complement this survey with overviews on models specifically designed for transactional memory systems. Finally, some recent research [Burckhardt et al. 2012; Cerone et al. 2015] adopted variants of the same framework used in this paper to propose axiomatic specifications of transactional consistency models.

### 5. CONCLUSION

In this work we presented an overview of the most relevant consistency models for non-transactional storage systems. Thanks to our methodical approach, we were able

to highlight subtle yet meaningful differences among consistency models, thus helping scholars and practitioners attain a better understanding of the tradeoffs involved.

To describe consistency semantics we adopted a mathematical framework based on graph theory and first-order logic. As first contribution of this work, we developed such formal framework as an extension of the one presented in [Burckhardt 2014]. The framework is comprehensive and useful in capturing different factors involved in the executions of a distributed storage system.

We used this framework to formulate formal definitions for the most popular of the over 50 consistency semantics we analyzed. For the rest of them, we presented informal descriptions which provide insights about their feature and relative strenghts. Moreover, thanks to the axiomatic approach we adopted, we laid out a clustering of semantics according to criteria which account for their natures and common traits. In turn, both the clustering and the formal definitions helped us building a partial ordering of consistency models (see Figure 1). We believe this partial ordering of semantics will prove convenient both in designing more precise and coherent models, and in evaluating and comparing the correctness of systems already in place. Finally, as further contribution, we provide in Appendix B an ordered list of all the models analyzed in this work, along with references to their definitions and main implementations in research literature.

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## A. SUMMARY OF CONSISTENCY PREDICATES

```
LINEARIZABILITY(\mathcal{F})
                                               SINGLEORDER \land REALTIME \land RVAL(\mathcal{F})
                                               \exists H' \subseteq \{op \in H : op.oval = \nabla\} : vis = ar \setminus (H' \times H)
SINGLEORDER
REALTIME
                                               rb \subseteq ar
Regular(\mathcal{F})
                                               SINGLEORDER \land REALTIMEWRITES \land RVAL(\mathcal{F})
SAFE(\mathcal{F})
                                               SINGLEORDER \land REALTIMEWRITES \land SEQRVAL(\mathcal{F})
REALTIMEWRITES
                                               rb|_{wr \to op} \subseteq ar
SEQRVAL(\mathcal{F})
                                               \forall op \in H : Concur(op) = \emptyset \Rightarrow op.oval \in \mathcal{F}(op, cxt(A, op))
                                               EVENTUALVISIBILITY \(\lambda\) NOCIRCULARCAUSALITY \(\lambda\)
EVENTUAL CONSISTENCY (\mathcal{F})
                                               RVal(\mathcal{F})
                                               \forall a \in H, \forall [f] \in H/\approx_{ss} : |\{b \in [f] : (a \xrightarrow{rb} b) \land (a \xrightarrow{vis} b)\}| < \infty
EVENTUALVISIBILITY
NOCIRCULARCAUSALITY
                                               acyclic(hb)
                                               \forall a, b \in H|_{rd} : vis^{-1}(a)|_{wr} = vis^{-1}(b)|_{wr} \Rightarrow a.oval = b.oval
STRONGCONVERGENCE
                                               EVENTUAL CONSISTENCY (\mathcal{F}) \wedge STRONG CONVERGENCE
STRONGEVENTUALCONS.(\mathcal{F})
                                               |H|_{wr}| < \infty \Rightarrow \exists C \in \mathcal{C} : \forall [f] \in H/\approx_{ss} : |\{op \in [f] : \}|
QUIESCENTCONSISTENCY(\mathcal{F})
                                               |op.oval \notin \mathcal{F}(op,C)\}| < \infty
PRAM
                                               so \subseteq vis
SEQUENTIAL CONSISTENCY (\mathcal{F})
                                               SINGLEORDER \land PRAMCONSISTENCY \land RVAL(\mathcal{F})
```

| $   \forall a \in H, \forall b, c \in H _{rd} : a \xrightarrow{\text{vis}} b \land b \xrightarrow{\text{so}} c \Rightarrow a \xrightarrow{\text{vis}} c \triangleq (vis; so _{rd \rightarrow rd}) \subseteq vis $  |
|--|
| $\forall a \in H _{wr}, \forall b \in H _{rd} : a \xrightarrow{\text{so}} b \Rightarrow a \xrightarrow{\text{vis}} b \triangleq so _{wr \to rd} \subseteq vis$   |
| $\forall a, b \in H _{wr} : a \xrightarrow{\text{so}} b \Rightarrow a \xrightarrow{\text{ar}} b \triangleq so _{wr \to wr} \subseteq ar$   |
| $ \forall a, c \in H _{wr}, \forall b \in H _{rd} : a \xrightarrow{\text{vis}} b \wedge b \xrightarrow{\text{so}} c \Rightarrow a \xrightarrow{\text{ar}} c \triangleq (vis; so _{rd \to wr}) \subseteq ar $   |
| $hb \subseteq vis$   |
| $hb \subseteq ar$  |
| $Causal V is ibility \land Causal Arbitration \land RVal(\mathcal{F})$   |
| $Causality(\mathcal{F}) \land StrongConvergence$   |
| $	ext{Causality}(\mathcal{F}) \wedge 	ext{RealTime}$   |
| $\forall a \in H _{wr}, \forall b \in H, \forall t \in Time : a.rtime = t \land b.stime =$   |
| $t + \Delta \Rightarrow a \xrightarrow{\text{vis}} b$  |
| $CAUSALITY(\mathcal{F}) \wedge TIMEDVISIBILITY(\Delta)$  |
| $SINGLEORDER \wedge TIMEDVISIBILITY(\Delta) \wedge RVAL(\mathcal{F})$  |
| $\textbf{SINGLEORDER} \land \textbf{MONOTONICWRITES} \land \textbf{RVAL}(\mathcal{F})$   |
| $SINGLEORDER \wedge REALTIMEWW \wedge RVAL(\mathcal{F})$   |
| $ rb _{wr 	o wr} \subseteq ar$   |
| $\begin{array}{c} \textbf{SINGLEORDER} \land \textbf{REALTIMEWW} \land \\ \textbf{K-REALTIMEREADS}(K) \land \textbf{RVAL}(\mathcal{F}) \end{array}$  |
| $\forall a \in H _{wr}, \forall b \in H _{rd}, \forall PW \subseteq H _{wr}, \forall pw \in PW :  PW  <$   |
| $K \wedge a \xrightarrow{ar} pw \wedge pw \xrightarrow{rb} b \wedge a \xrightarrow{rb} b \Rightarrow a \xrightarrow{ar} b$   |
| $PRAM \wedge REALTIME \wedge NoJoin \wedge RVAL(\mathcal{F})$  |
| $ \forall a_i, b_i, a_j, b_j \in H : a_i \not\approx_{ss} a_j \land (a_i, a_j) \in ar \setminus vis \land a_i \preceq_{so} b_i \land a_j \preceq_{so} b_j \Rightarrow (b_i, b_j), (b_j, b_i) \notin vis $  |
| $\begin{array}{c} READYOURWRITES \land REALTIME \land ATMOSTONEJOIN \land \\ RVAL(\mathcal{F}) \end{array}$  |
| $\forall a_i, a_j \in H : a_i \not\approx_{ss} a_j \land (a_i, a_j) \in ar \setminus vis \Rightarrow  \{b_i \in H : vis \neq a_i\}  $  |
| $   a_i \preceq_{so} b_i \wedge (\exists b_j \in H : a_j \preceq_{so} b_j \wedge b_i \xrightarrow{vis} b_j )   \leq 1 \wedge  \{b_j \in H : b_j \in H$ |
| $ a_j \preceq_{so} b_j \wedge (\exists b_i \in H : a_i \preceq_{so} b_i \wedge b_j \xrightarrow{vis} b_i)  \le 1$  |
| $PRAM \wedge NOJOIN \wedge RVAL(\mathcal{F})$ $PRAM \wedge NOJOIN \wedge RVAL(\mathcal{F})$  |
| $\begin{array}{c} PRAM \land K\text{-}REALTIME(2) \land ATMOSTONeJOIN \land RVAL(\mathcal{F}) \\ \\ \end{array}$   |
| $(so \cap ob) \subseteq vis$   |
| $\exists H' \subseteq \{op \in H : op.oval = \nabla\} : ar \cap ob = vis \cap ob \setminus (H' \times H)$  |
| $\begin{array}{c} \textbf{PEROBJECTSINGLEORDER} \land \textbf{PEROBJECTPRAM} \land \\ \textbf{RVal}(\mathcal{F}) \end{array}$  |
| $PEROBJECTSINGLEORDER \land PRAM \land RVAL(\mathcal{F})$  |
| $hbo \triangleq ((so \cap ob) \cup vis)^+$   |
|  |

 $\it Table II: Summary of consistency predicates listed in the paper.$ 

## **B. PRIMARY REFERENCES**

| Models                      | Definitions                                       | Implementations <sup>13</sup>   |
|-----------------------------|---|---|
| Atomicity                   | [Lamport 1986b]                                   | [Attiya et al. 1995]  |
| Bounded fork-join           | [Mahajan et al. 2011]                             | -   |
| causal<br>Bounded staleness | [Mahajan et al. 2010]                             | -   |
| Causal                      | [Lamport 1978; Hutto and                          | [Ladin et al. 1992; Birman  |
|                             | Ahamad 1990; Ahamad et al.                        | et al. 1991; Lakshmanan   |
| Causal+                     | 1995; Mahajan et al. 2011] [Lloyd et al. 2011]    | et al. 2001; Lloyd et al. 2013;<br>Du et al. 2014; Zawirski et al.<br>2015; Lesani et al. 2016]<br>[Petersen et al. 1997; |
|                             |   | Belaramani et al. 2006;<br>Almeida et al. 2013]   |
| Coherence                   | [Dubois et al. 1986]                              | -   |
| Conit                       | [Yu and Vahdat 2002]                              | -   |
| $\Gamma$ -atomicity         | [Golab et al. 2014]                               | -   |
| $\Delta$ -atomicity         | [Golab et al. 2011]                               | -   |
| Delta                       | [Singla et al. 1997]                              | -   |
| Entry                       | [Bershad and Zekauskas                            | -   |
| T . 1                       | 1991]   | [D :]   |
| Eventual                    | [Terry et al. 1994; Vogels 2008]                  | [Reiher et al. 1994; DeCandia et al. 2007; Singh et al. 2009;   |
|                             | 2008]   | Bortnikov et al. 2010;  |
|                             |   | Bronson et al. 2013]  |
| Eventual                    | [Serafini et al. 2010]                            | -   |
| linearizability             |   |   |
| Eventual                    | [Fekete et al. 1996]                              | -   |
| serializability             | [I : 1 M: \                                       | [F-1]   |
| Fork*                       | [Li and Mazières 2007]                            | [Feldman et al. 2010]   |
| Fork                        | [Mazières and Shasha 2002;<br>Cachin et al. 2007] | [Li et al. 2004;<br>Brandenburger et al. 2015]  |
| Fork-join causal            | [Mahajan et al. 2010]                             | - Drandenburger et al. 2015]  |
| Fork-sequential             | [Oprea and Reiter 2006]                           | _   |
| Hybrid                      | [Attiya and Friedman 1992]                        | _   |
| K-atomic                    | [Aiyer et al. 2005]                               | _   |
| K-regular                   | [Aiyer et al. 2005]                               | _   |
| K-safe                      | [Aiyer et al. 2005]                               | _   |
| k-staleness                 | [Bailis et al. 2012]                              | _   |
| Lazy release                | [Keleher et al. 1992]                             | _   |
| Linearizability             | [Herlihy and Wing 1990]                           | [Burrows 2006; Baker et al.   |
| 211100112001110)            | [Indiana wing root]                               | 2011; Glendenning et al.  |
|                             |   | 2011; Calder et al. 2011;   |
|                             |   | Corbett et al. 2013; Han et al.   |
| т                           | [C 1 C 1 C C C C C C C C C C C C C C C C          | 2015; Lee et al. 2015]  |
| Location                    | [Gao and Sarkar 2000]                             | - I 10053   |
| Monotonic reads             | [Terry et al. 1994]                               | [Terry et al. 1995]   |

 $<sup>\</sup>overline{^{13}}$ In case of very popular consistency semantics (e.g., causal consistency, atomicity/linearizability), we only cite a subset of known implementations.

| Monotonic writes                      | [Terry et al. 1994]             | [Terry et al. 1995]   |
|---------------------------------------|---------------------------------|---|
| Observable causal                     | [Attiya et al. 2015]            | -   |
| PBS $\langle k, t \rangle$ -staleness | [Bailis et al. 2012]            | -   |
| Per-object causal                     | [Burckhardt et al. 2014]        | _   |
| Per-record timeline                   | [Cooper et al. 2008; Lloyd      | [Andersen et al. 2009]                                      |
|                                       | et al. 2011]                    |   |
| PRAM                                  | [Lipton and Sandberg 1988]      | -   |
| Prefix                                | [Terry et al. 1995; Terry       | -   |
| D                                     | 2013]<br>  [Goodman 1989]       |   |
| Processor                             |                                 | -   |
| Quiescent                             | [Herlihy and Shavit 2008]       | -   |
| Rationing                             | [Kraska et al. 2009]            | -<br>   |
| Read-your-writes                      | [Terry et al. 1994]             | [Terry et al. 1995]   |
| Real-time causal                      | [Mahajan et al. 2011]           | -   |
| RedBlue                               | [Li et al. 2012]                |   |
| Regular                               | [Lamport 1986b]                 | [Malkhi and Reiter 1998a;<br>Guerraoui and Vukolic 2006]    |
| Release                               | [Gharachorloo et al. 1990]      | -   |
| Safe                                  | [Lamport 1986b]                 | [Malkhi and Reiter 1998b;<br>Guerraoui and Vukolic 2006]    |
| Scope                                 | [Iftode et al. 1996b]           | -   |
| Sequential                            | [Lamport 1979]                  | [Rao et al. 2011]   |
| Slow                                  | [Hutto and Ahamad 1990]         | -   |
| Strong eventual                       | [Shapiro et al. 2011a]          | [Shapiro et al. 2011b; Conway et al. 2012; Roh et al. 2011] |
| Timed causal                          | [Torres-Rojas and Meneses 2005] | -   |
| Timed serial                          | [Torres-Rojas et al. 1999]      | -   |
| Timeline                              | [Cooper et al. 2008]            | [Rao et al. 2011]   |
| Tunable                               | [Krishnamurthy et al. 2002]     | [Lakshman and Malik 2010;                                   |
|                                       | , v                             | Wu et al. 2013; Perkins et al.                              |
|                                       |                                 | 2015; Sivaramakrishnan                                      |
|                                       | FD 11                           | et al. 2015]  |
| t-visibility                          | [Bailis et al. 2012]            | -   |
| Vector-field                          | [Santos et al. 2007]            | -   |
| Weak                                  | [Vogels 2008; Bermbach and      | -   |
| 777 1                                 | Kuhlenkamp 2013]                | [0]   |
| Weak<br>fork-linearizability          | [Cachin et al. 2011]            | [Shraer et al. 2010]  |
| Weak ordering                         | [Dubois et al. 1986]            |   |
| Writes-follow-reads                   | [Terry et al. 1994]             | [Terry et al. 1995]   |
| willes-lullow-reads                   | [1611 y et al. 1334]            | [1611 y et al. 1333]  |

 $\it Table\ IV:$  Definitions of consistency semantics and some of their implementations in literature.